1 INTRODUCTION
Nearly all of the software we use today is part of a distributed system. Apps on your phone participate with hosted services in the cloud; together they form a distributed system. Hosted services themselves are massively distributed systems, often running on machines spread across the globe. “Big data” systems and enterprise databases are distributed across many machines. Most scientific computing and machine learning systems work in parallel across multiple processors. Even legacy desktop operating systems and applications like spreadsheets and word processors are tightly integrated with distributed backend services.

Distributed systems are tricky, so their ubiquity should worry us. Multiple unreliable machines are running in parallel, sending messages to each other across network links with arbitrary delays. How can we be confident that our programs do what we want despite this chaos?

This problem is urgent, but it is not new. The traditional answer has been to reduce this complexity with memory consistency guarantees: assurances that the accesses to memory (heap variables, database keys, etc) occur in a controlled fashion. However, the mechanisms used to enforce these guarantees—coordination protocols—are often criticized as barriers to high performance, scale and availability of distributed systems.

1.1 The High Cost of Coordination
Coordination protocols enable autonomous, loosely coupled machines to jointly decide how to control basic behaviors, including the order of access to shared memory. These protocols are among the most clever and widely cited ideas in distributed computing. Some well-known techniques include the Paxos and Two-Phase Commit protocols, and global barriers underlying computational models like Bulk Synchronous Processing.

Unfortunately, the expense of coordination protocols can make them “forbidden fruit” for programmers. James Hamilton from Amazon Web Services made this point forcefully, using the phrase “consistency mechanisms” where we use coordination:

The first principle of successful scalability is to batter the consistency mechanisms down to a minimum, move them off the critical path, hide them in a rarely visited corner of the system, and then make it as hard as possible for application developers to get permission to use them [27].

The issue is not that coordination is tricky to implement, though that is true. The main problem is that coordination can dramatically slow down computation, or stop it altogether. Recent work showed that state-of-the-art multiprocessor key-value stores can spend 90% of their time waiting for coordination; a coordination-free implementation called Anna ran over two orders of magnitude faster by eliminating that coordination [47]. Key-value stores are simple systems with narrow APIs. Can we avoid coordination more generally, as Hamilton recommends? When?

Surprisingly, this was an open question in distributed systems until relatively recently, due to a narrow focus on storage semantics. We can do better by moving up the stack, setting aside incidental storage details and considering program semantics more holistically. Before we delve into details, we begin with intuition on what is desirable and what is possible.

1.2 Stay in Your Lane: The Perfect Freeway
As an analogy, consider driving on a highway during rush hour. If each car would drive forward independently in its lane at the speed limit, everything would be fine: the capacity of the highway could be fully exploited. Unfortunately, there always seem to be drivers who have other places to go than forward! To prevent two cars from being in the same place at the same time, we drivers engage in various forms of coordination when entering traffic, changing lanes, coming to intersections, etc. We adhere to formal protocols, including traffic lights and stop signs. We also frequently engage in ad hoc forms of coordination with neighboring cars by using turn signals, eye contact, and the familiar but subtle dance of driving our vehicles more or less aggressively. With all these mechanisms, one thing is common: they slow us down when traffic is crowded. Worse, these slowdowns propagate back to the drivers behind us, and queuing effects amplify the problems. In the end, rush hour on the highway is a nightmare—wildly less efficient than the highway’s capacity.

The analogy to distributed systems is fairly direct. In principle, each machine or process in a system could proceed forward autonomously with its ordered list of instructions, and make progress as quickly as possible. But to avoid conflicts on shared state (akin to two cars being in the same place at the same time), distributed software employs coordination protocols to stay “safe”. The effect of these protocols is to cause one or more processes to idly wait until some other process successfully sends a signal saying it is done.

In many cases, however, coordination is not a necessary evil, it is an incidental requirement of a design decision. To return to our traffic analogy, consider stop lights: they allow drivers to mediate access to a shared intersection by following a waiting protocol. Stop light delays can be easily avoided by taking advantage of another dimension in space: an overpass or tunnel removes the intersection entirely. There is no endemic need to employ coordination in two dimensions via stop lights; they are just one engineering solution to a problem, with a particular tradeoff between cost of initial implementation and resulting throughput.

As it happens, humans are not very good at simply driving forward at a fixed speed in their lane; but machines are [43]!
Figure 1: A distributed waits-for graph with replicated nodes and partitioned edges. There are two cycles here: one local to Machine 1 (\{T_1, T_2\}), and one that spans Machines 1 and 2 (\{T_1, T_3\}).

**1.3 Cruising and Stalling on Graphs**

The Perfect Freeway is an idealistic analogy. We return our attention to examples from distributed computing, to illustrate when we can and cannot achieve the ideal of coordination-freeness. We consider two nearly identical classical distributed systems problems involving graph reachability—one coordination-free, one not.

### 1.3.1 Distributed Deadlock Detection

Distributed databases identify cycles in a distributed graph in order to detect and remediate deadlocks. In a traditional database system, a transaction \(T_i\) may be waiting for a lock held by another transaction \(T_j\), which may in turn be waiting for a second lock held by \(T_i\). The deadlock detector identifies such “waits-for” cycles by analyzing a directed graph in which nodes represent transactions, and edges represent one transaction waiting for another on a lock queue.

In a distributed database, a “local” (single-machine) view of the waits-for graph contains only a subset of the edges in the global waits-for graph. In this scenario, how do local deadlock detectors work together to identify global deadlocks?

Waits-for cycles may span machines, as in Figure 1. To identify these distributed deadlocks, each machine can exchange copies of its edges with other machines to accumulate more information about the global graph. Any time a machine observes a cycle in the information it has received so far, it can declare a deadlock among the transactions on that cycle.

We might be concerned that there are “race conditions” in this distributed computation. Do local detectors have to coordinate with other nodes to be sure of a deadlock they have observed? In this case, no coordination is required. To see this, note that decisions based on incomplete information are stable. For example, once Machine 1 and Machine 2 jointly identify a deadlock between \(T_1\) and \(T_3\), new information from Machine 3 will not change that fact. Additional facts can only result in additional cycles being detected: the output grows monotonically with the input. Finally, if all the edges are eventually shared across all machines, the machines will agree upon the outcome, which is based on the full graph.

### 1.3.2 Distributed Garbage Collection

Garbage collectors in distributed systems must identify unreachable objects in a distributed graph of memory references. Garbage collection works by identifying graph components that are disconnected from the “root” of a system runtime.

In a distributed system, references to objects can span machines. A local view of the reference graph contains only a subset of the edges in the global graph. How can multiple local garbage collectors work together to identify objects that are truly unreachable?

Note that a machine may have a local object and no knowledge whether the object is connected to the root—Machine 3 and object \(O_4\) in Figure 2 form an example. Yet there still may be a path to that object from the root that consists of edges distributed across other machines. Hence machines should exchange copies of edges to accumulate more information about the graph.

As before, we might be concerned that there are race conditions here. Can local collectors autonomously declare and deallocate garbage? Here, the answer is different: coordination is indeed required! To see this, note that a decision based on incomplete information—e.g., Machine 3 deciding that object \(O_4\) is unreachable in Figure 2—can be invalidated by the subsequent arrival of new information that demonstrates reachability (e.g., the edges Root \(\rightarrow\) \(O_4\), \(O_1\) \(\rightarrow\) \(O_3\), \(O_3\) \(\rightarrow\) \(O_4\)). The output does not grow monotonically with the input: previous “answers” may need to be retracted! To avoid this, a machine must ensure that it has heard everything there is to hear before it declares an object unreachable. The only way to know it has heard everything is to coordinate with all the other machines to establish that fact.

**1.4 The Crux of Consistency: Monotonicity**

These examples bring us back to our fundamental question, which applies to any concurrent computing framework:

**Question:** What is the family of problems that can be consistently computed in a distributed fashion without coordination, and what problems lie outside that family?

There is a difference between an incidental use of coordination and an intrinsic need for coordination: the former is the result of an implementation choice; the latter is a property of a computational problem. Hence our Question is one of computability, like P vs. NP or Decidability. It asks what is (im)possible for a clever programmer to achieve.

Note that the question assumes some definition of “consistency”. Where traditional work focused narrowly on memory consistency (i.e., reads and writes produce agreed-upon values), we want to focus on program consistency: does the program produce the outcome...
we expect (e.g., deadlocks detected, garbage collected), despite any race conditions that might arise?

Our examples provide clues for answering our question. Both depend on graph reachability, but they differ in one key aspect. A deadlock is identified by the existence of a (cyclic) path. Garbage is identified by the non-existence of a path. The set of satisfying paths that exist is monotonic in the information received:

**Definition 1.** A program $P$ is monotonic if for any input sets $S, T$ where $S \subseteq T$, $P(S) \subseteq P(T)$.

By contrast, the set of satisfying paths that do not exist is non-monotonic: conclusions made on partial information may not hold in eventuality.

Monotonicity is the key property underlying the need for coordination to establish consistency, as captured in the CALM Theorem:

**Theorem 1.** Consistency As Logical Monotonicity (CALM). A program has a consistent, coordination-free distributed implementation if and only if it is monotonic.

Intuitively, monotonic programs are "safe" in the face of missing information, and can proceed without coordination. Non-monotonic programs, by contrast, must be concerned that truth of a property could change in the face of new information. Therefore they cannot proceed until they know all information has arrived, requiring them to coordinate.

Additionally, because they "change their mind", non-monotonic programs are order-sensitive: the order in which they receive information determines how they toggle state back and forth, which in turn determines their final state. By contrast, monotonic programs simply accumulate beliefs; their output depends only on the content of their input, not the order in which is arrives.

Our discussion so far has remained at the level of intuition. The next section provides a sketch of a proof of the CALM Theorem, including further discussion of definitions for consistency and coordination. Those seeking a formal proof are directed to the papers by Ameloot, et al. [8, 9].

## 2 CALM: A PROOF SKETCH

Our first challenge in formalizing the CALM Theorem is to define program consistency in a manner that allows us to reason about program outcomes, rather than mutations to storage. Having done that, we can move on to a proof that is more refined than those based on traditional memory consistency.

### 2.1 Program Consistency: Confluence

Distributed systems introduce significant non-determinism to our programs. Sources of non-determinism include unsynchronized parallelism, unreliable components, and networks with unpredictable delays. As a result, a distributed program can exhibit a large space of possible behaviors on a given input.

While we may not control all the behavior of a distributed program, our true concern is with its observable behavior: the program outcomes. To this end, we want to assess how distributed non-determinism affects program outcomes. A practical consistency question is this: "Does my program produce deterministic outcomes despite non-determinism in the runtime system?"

This is a question of program confluence. In the context of non-deterministic message delivery, an operation on a single machine is confluent if it produces the same set of outputs for any non-deterministic ordering and batching of a set of inputs. Following our discussion of sets of information $S$ and $T$ above, a confluent single-machine operation can be viewed as a deterministic function from sets to sets, abstracting away the nondeterministic order in which its inputs happen to appear in a particular run of a distributed system. Confluent operations compose: if the outputs of one confluent operation are consumed by another, the resulting composite operation is confluent. Hence confluence can be applied to individual operations, components in a dataflow, or even entire distributed programs [2]. If we restrict ourselves to building programs by composing confluent operations, our programs are confluent by construction, despite orderings of messages or execution races within and across components.

Unlike traditional memory consistency properties from the systems literature such as linearizability [30] and serializability [21], confluence makes no requirements or promises regarding notions of recency (e.g., a read is not guaranteed to return the result of the latest write request issued) or ordering of operations (e.g., writes are not guaranteed to be applied in the same order at all replicas). Nevertheless, if an application is confluent, we know that any such anomalies at the memory or storage level do not affect the application outcomes.

Confluence is a powerful yet permissive correctness criterion for distributed applications. It rules out application-level inconsistency due to races and non-deterministic delivery, while permitting non-deterministic ordering and timings of lower-level operations that may be costly (or sometimes impossible) to prevent in practice.

### 2.1.1 Confluent Shopping Carts

To illustrate the utility of reasoning about confluence, we consider an example of a higher-level application. In their paper on the Dynamo key-value store [20], researchers from Amazon describe a shopping cart application that achieves confluence without coordination. In their scenario, a client web browser requests items to add and delete from an online shopping cart. For availability and performance, the state of the cart is tracked by a distributed set of server replicas, which may receive requests in different orders. In the Amazon implementation, shopping performs no coordination, yet all server replicas eventually reach the same final state. The shopping cart is precisely the class of program that interests us: eventually consistent, even when implemented atop a non-deterministic distributed substrate that does no coordination.

Program consistency is possible in this case because the fundamental operations performed on the cart (e.g., adding items) commute, so long as the contents of the cart are represented as a set and the internal ordering of its elements is ignored. If two replicas disagree about the contents of the cart, their differing views can be reconciled simply by taking the union of their respective sets.

A complication in this context is that deletes are not monotonic and seem to cause consistency trouble: if instructions to add item 1 and delete item 1 arrive in different orders at different machines, the machines may disagree on whether 1 should be in the cart. As a traditional approach to avoid such "race conditions", we might...
work with one machine’s state and event loop shown in de-
a relational backing store and programs written as queries. Each
Simply put, a relational transducer is an event-driven server with
relational transducer
monotonic (or non-monotonic) logic, Ameloot uses the formalism
briefly review the structure of the argument from Ameloot, et al.
In a subsequent series of papers [8, 9, 48], Ameloot and
2010 and written up shortly thereafter alongside a number of corol-
laries [29]. In a subsequent series of papers [8, 9, 48], Ameloot and
broader challenge is to formally define “coordination” messages, and distin-
guish them from other forms of message passing that satisfy data
dependencies needed to compute an output. To do this, Ameloot,
et al. consider all possible ways to partition data across machines
in the network at program start. From each of these starting points,
a messaging pattern is produced during execution of the program.
We say that a program contains coordination if it requires messages
to be sent under all possible partitionings— including partitionings
that co-locate all data at a single machine. Any message that is sent
involves minimizing the use of such protocols.

2.2 A Sketch of The Proof
The CALM conjecture was presented in a keynote talk at PODS
2010 and written up shortly thereafter alongside a number of corol-
laries [29]. In a subsequent series of papers [8, 9, 48], Ameloot and
colleagues presented a formalization and proof of the CALM Theo-
rem which remains the reference formalism at this time. Here we
brieﬂy review the structure of the argument from Ameloot, et al.
To capture the notion of a distributed system composed out of
monotonic (or non-monotonic) logic, Ameloot uses the formalism of
a relational transducer [1] running on each machine in a network.
Simply put, a relational transducer is an event-driven server with
a relational backing store and programs written as queries. Each
transducer runs a sequential event loop as follows:

(1) Ingest and apply an unordered batch of requests to insert
deletes records in local relations. Requests may come
from other machines or a distinguished input relation.
(2) Query the (now-updated) local relations to compute batches
of records that should be sent somewhere (possibly locally)
for handling in future.
(3) Send the results of the query phase to relevant machines in
the network as requests to be handled. Results sent locally
are ingested in the very next iteration of the event loop.
Results can also be “sent” to a distinguished output.

The Send phase knows where to send records based on their
data content: the records contain addresses of other machines in
the network. In essence, a programmer in this environment “issues
a request to send a message to machine n” by causing a record
containing the address of n to be ingested, and writing a Query that
will read that record and generate the relevant output for the Send
phase.

The next challenge is to deﬁne monotonicity carefully. In Re-
lational Transducers, "programs expressible in monotonic logic"
are easy to deﬁne: they are the transducer networks where every
machine’s queries are syntactically monotonic relational queries.
For instance, in the relational algebra, we can allow each machine
to employ selection, projection, intersection, join and transitive
closure (the monotonic operators of relational algebra), but not
set-diﬀerence (the sole non-monotonic operator). If we use rela-
tional logic, we disallow the use of universal quantifiers (V )
and their negation-centric equivalent (~3)—precisely the construct that
tripped us up in the garbage collection example of Section 1.3.2
("everything there is to hear"). If we model our programs with mu-
table relations, insertions are allowable, but in general updates and
deletions are not [5, 35]. These informal descriptions elide a num-
er of clever exceptions to these rules that still achieve semantic
monotonicity despite syntactic non-monotonicity [8, 18], but they
give a sense of how the formalism is deﬁned.

Now that we have a formal execution model (relational trans-
ducers), a deﬁnition of consistency (conﬂuence), and a deﬁnition
of monotonic programs, we are prepared to prove a version of the
CALM Theorem. The forward “if” direction of the CALM Theorem
is quite straightforward and similar to our previous discussion: it is
easy to show that any monotonic relational transducer in the
network will eventually Ingest and Send a deterministic set of mes-
ages, and generate a deterministic output.

The reverse “only if” direction is quite a bit trickier, as it requires
ruled out any possible scheme for avoiding coordination. The ﬁrst
challenge is to formally deﬁne “coordination” messages, and distin-
guish them from other forms of message passing that satisfy data
dependencies needed to compute an output. To do this, Ameloot,
et al. consider all possible ways to partition data across machines
in the network at program start. From each of these starting points,
a messaging pattern is produced during execution of the program.
We say that a program contains coordination if it requires messages
to be sent under all possible partitionings— including partitionings
that co-locate all data at a single machine. Any message that is sent

\[3\] This paradigm has been used in a number of languages for Declarative Networking
like Overlog and NDlog [37, 38], as well as in the Bloom language for distributed
programming [3].
in every partitioning is a coordination message. As an example, consider how a distributed garbage collector decides if a locally disconnected object \( O_g \) is garbage. Even if all the data is placed at a single machine, that machine needs to exchange messages with the other machines to check that they have no more additional edges—it needs to "coordinate", not just communicate data dependencies. The proof then proceeds to show that non-monotonic operations require this kind of coordination.

This brief description elides many interesting aspects of the original paper. In addition to the connections established between monotonicity and coordination-freeness, connections are also made between these properties and other distributed systems properties. Of particular note is the issue of distributed agreement on network membership (represented by Ameloot, et al. as the \( \text{All} \) relation). Network membership is a classic challenge in distributed systems, and the complicating factor in many classic distributed protocols. It is shown that the class of monotonic programs is the same as the class of programs that do not require knowledge of network membership—they do not query \( \text{All} \). A similar connection is shown with the property of a machine being aware of its own identity/address (querying the \( \text{Id} \) relation).

3 CALM PERSPECTIVE ON THE STATE OF THE ART

The CALM theorem describes what is and is not possible. But can we use it practically? In this section, we address the implications of CALM with respect to the state of the art in distributed systems practice. It turns out that many patterns for maintaining consistency follow directly from the theorem.

3.1 CAP and CALM: Going Positive

Brewer’s CAP Theorem [14] informally states that a system can exhibit only two out of the three following properties: Consistency, Availability, and Partition-tolerance. CAP is a negative result: it captures consistency properties that cannot be achieved in general. But Brewer frames this with constructive advice:

[The original] expression of CAP served its purpose, which was to open the minds of designers to a wider range of systems and tradeoffs ... The modern CAP goal should be to maximize combinations of consistency and availability that make sense for the specific application. [14]

CALM is a positive result in this arena: it circumscribes the class of programs for which all three of the CAP properties can indeed be achieved simultaneously. To see this, note the following:

Observation 1. Coordination-freeness is equivalent to availability under partition.

In the forward direction, a coordination-free program is by definition available under partition: all machines can proceed independently. When and if the partition heals, state merger is monotonic and consistent. In the reverse direction, a program that employs coordination will stall (become unavailable) during coordination protocols if the machines involved in the coordination span the partition.

In that frame, CALM asks and answers the underlying question of CAP: "which programs can be consistently computed while remaining available under partition?". CALM does not contradict CAP. Instead, CALM approaches distributed consistency from a wider frame of reference:

1. First, CAP is a negative result over the space of all programs: CALM confirms this coarse result, but delineates at a finer grain the negative and positive cases. Monotone programs can in fact satisfy all three of the CAP properties at once; non-monotone programs are the ones that cannot.

2. The key insight in CALM is to focus on consistency from the viewpoint of program outcomes rather than the traditional histories of storage mutation. The emphasis on the program being computed shifts focus from implementation to specification: it allows us to ask questions about what computations are possible.

The latter point is what motivated our outcome-oriented definition of program consistency. Where the CAP Theorem proofs of Gilbert and Lynch [24] choose linearizability of updates to storage, the CALM Theorem proofs choose confluence of program outcomes. We note that confluence is both more permissive and closer to user-observable properties. CALM provides the formal framework for the widespread intuition that we can indeed "work around CAP" in many cases, even if we violate traditional systems-level notions of storage consistency.

3.2 Distributed Design Patterns

Our shift of focus from mutable storage to program semantics has implications beyond proofs. It also informs the design of better programming paradigms for distributed computing.

Traditional programming models the world as a collection of named variables whose values change over time. Bare assignment [10] is a nonmonotonic programming construct: outputs based on a prefix of assignments may have to be retracted when new assignments come in. Similarly, assignments make final program states dependent upon the arrival order of inputs. This makes it extremely hard to take advantage of the CALM theorem to analyze systems written in traditional imperative languages!

Functional programming has long promoted the use of immutable variables, which are constrained to take on only a single value during a computation. Viewed through the lens of CALM, an immutable variable is a simple monotonic pattern: it transitions from being undefined to its final value, and never goes back. Immutable variables generalize to immutable data structures; techniques such as deforestation [45] make programming with immutable trees, lists and graphs practical.

Monotonic programming patterns are common in the design of distributed storage systems. We already discussed the Amazon shopping cart for Dynamo, which models cart state as two growing sets. A related pattern in storage systems is the use of tombstones: special data values that mark a data item as deleted. Instead of explicitly allowing deletion (a non-monotonic construct), tombstones masked immutable values with corresponding immutable tombstone values. Taken together, a data item with tombstone monotonically transitions from undefined, to a defined value, and ultimately to tombstoned.
Conflict-free replicated data types (CRDTs) [42] provide an object-oriented framework for monotonic programming patterns like tombstones, typically for use in the context of replicated state. A CRDT is an abstract data type whose internal state is a lattice that evolves monotonically according to a partial order, such as the partial order of set containment under \( \subseteq \) or of integers under \( \leq \). Two replicas of a CRDT converge to the same state regardless of the order of their inputs. Equally importantly, the states of two CRDT replicas that may have seen different inputs and orders can always be deterministically merged into a new final state that incorporates all of the inputs seen by both.

CRDTs are an OO lens on a long tradition of prior work that exploits commutativity to achieve determinism under concurrency. This goes back at least to long-running transactions [16, 23], continuing through recent work on the Linux kernel [17]. The benefits of commutativity have motivated not only abstract data types, but also composable libraries or languages, enabling programmers to reason about correctness of whole programs [3, 34, 39]. We turn to an example of that idea next.

### 3.3 The Bloom Programming Language

One way to encourage good distributed design patterns is to use a language specifically centered around those patterns. Bloom is a programming language we designed in that vein.

The main goal of Bloom is to make distributed systems easier to reason about and program. We felt that a good language for a domain is one that obscures irrelevant details and brings into sharp focus those that matter. Given that data consistency is a core challenge in distributed computing, we designed Bloom to be data-centric: both system state and events are represented as named data, and computation is expressed as queries over that data. The programming model of Bloom closely resembles that of the relational transducers described in Section 2.2. From the programmer’s perspective, Bloom resembles event-driven or actor-oriented programming—Bloom programs use reorderable query-like handler statements to describe how an agent responds to messages (represented as data) by reading and modifying local state and by sending messages.

Because Bloom programs are written in a relational-style query language, monotonicity is easy to spot just as it was in relational transducers. The relatively uncommon non-monotonic operations such as anti-join and set minus stand out in the language’s syntax. In addition, Bloom’s types include CRDT-like lattices that provide object-level commutativity, associativity and idempotence.

The advantages of the Bloom design are twofold. First, Bloom makes set-oriented, monotonic (and hence confluent) programming the easiest constructs for programmers to work with in the language. Contrast this with imperative languages, in which assignment and explicit sequencing of instructions—two non-monotone constructs!—are the most natural and familiar building blocks for programs. Second, Bloom can leverage static analysis based on CALM to certify when programs provide the state-based convergence properties provided by CRDTs, and when those properties are preserved across compositions of modules. This is the power of a language-based approach to monotonic programming: local, state-centric guarantees can be automatically composed into global, outcome-oriented, program-level guarantees.

With Bloom as a base, we have developed tools including declarative testing frameworks [4], verification tools [6], and program transformation libraries that add coordination to programs that cannot be statically proven to be confluent [2].

### 3.4 Coordination In Its Place

Pragmatically, it can be difficult to find a monotonic implementation of a full-featured application. Instead, a good strategy is to keep coordination off of the critical path. In the shopping cart example, coordination was limited to checkout, when user performance expectations are lower. In the garbage collection example (assuming adequate resources) the task can run in the background without affecting users.

It can take creativity to move coordination off of the critical path and into a background task. The most telling example from Section 3.2 is the use of tombstoning for low-latency deletion. In practice, memory for tombstoned items must be reclaimed, so eventually all machines need to agree to delete some items. Like GC, this distributed deletion can be coordinated lazily in the background on a rolling basis. In this case, monotonic design does not stamp out coordination entirely, it moves it off the critical path.

Another non-obvious use of CALM analysis is to identify when to compensate (“apologize” [28]) for inconsistency, rather than prevent it via coordination. For example, when a retail site allows you to purchase an item, it should decrement the count of items in inventory. This non-monotonic action suggests that coordination is required, e.g., to ensure that the supply is not depleted before an item is allocated to you. In practice, this requires too much integration between systems for inventory, supply chain, and shopping. In the absence of such coordination, your purchase may fail non-deterministically after checkout. To account for this possibility, additional compensation code must be written to detect the out-of-stock exception, and handle it by—for example—sending you an apologetic email with a loyalty coupon. Note that a coupon is not a clear mathematical inverse of any action in the original program; domain-aware compensation often goes beyond typical type system logic.

In short, we do not advocate pure monotonic programming as the only way to build efficient distributed systems. Monotonicity also has utility as an analysis framework for identifying non-determinism so that programmers can address it creatively.

### 4 Questions

The CALM Theorem provides a “bright line” between problems that require coordination and those that do not. In addition to the constructive directions sketched above, CALM also raises a number of questions at the heart of distributed systems theory and practice.

#### 4.1 Expressiveness

Typically, when we define a family of computations, we expect a characterization of the expressive power of that family. What is the expressive power of the monotone distributed programs from the CALM Theorem?
This is a question of descriptive complexity, and one landmark result in that space is the Immerman-Vardi Theorem [31, 44]. In a nutshell, Immerman-Vardi states that if you take a suitably defined class of monotone logic programs (where negation is allowed only on pre-defined, stored relations) and provide some successor relation that provides a total order, the resulting language can express all of PTIME.

So one natural question is this: can we implement all of PTIME in a coordination-free manner? Do the conditions of the Immerman-Vardi Theorem align with the conditions of the CALM Theorem?

Intuitively, the answer would appear to be “no.” One concern is that Immerman-Vardi’s requirement for a successor relation is an unreasonable assumption for a distributed system. Indeed, coordination protocols like Paxos were designed precisely to achieve such a totally ordered sequence in a distributed system. But what if we made different, pragmatic assumptions about what can be assumed in a distributed systems: e.g. a successor relation per node, and causal ordering across nodes? How large a complexity class could we achieve? The specifics of the definitions of the computing model and desired guarantees are critical to the question of what is achievable.

The state of the art in this direction is captured by Ameloot and Van den Bussche [7]. For example, if all machines know the rules for partitioning data across the system, certain syntactically non-monotone programs can be treated as monotone and run coordination-free. It would seem plausible that the class of programs that can be practically made coordination-free could be expanded even further with other common system assumptions.

4.2 Monotonic Program Synthesis

The CALM Theorem is not a constructive result: it provides no assistance in finding monotonic implementations of programs. Perhaps such programs are difficult for developers to discover?

In this setting, it is interesting to consider program synthesis techniques. Monotone relational languages seem well-suited, because they are small yet expressive. There is encouraging work in this regard. Cheung and colleagues [15] have had success lifting imperative code fragments in traditional programming languages into declarative, monotonic SQL code. Going further, Itzhaky and colleagues show how to synthesize more complex logic programs that correspond to more expressive complexity classes [32]. With such techniques, perhaps most programmers could stick with traditional languages, and have their code translated into something like Bloom to get the attendant benefits.

Cheung’s group has also had success at synthesizing SQL queries from input/output examples [46]. As we look forward to a world where machine learning replaces some of the trickiness and tedium of programming, perhaps logic languages with a focus on monotonicity should be a key target for efficient distributed systems.

4.3 Analyzing Non-Monotonic Code

In logic languages like Bloom, it is easy to (conservatively) certify programs as deterministic if they only use monotonic syntax. A programmer or compiler can “repair” non-monotonic statements by wrapping them with coordination logic. But the resulting repaired code still contains non-monotonic statements. Can we write program checks that will verify the consistency of such code?

One underlying challenge here is that coordination does not remove non-determinism, it controls non-determinism across the system. For example, Paxos is often used to impose an order for concurrent events in a distributed system; this ensures uniform decisions across machines in one run of the system, but another run might produce a different outcome. Hence our definition of consistency as confluence does not precisely capture the effect of coordination in non-monotonic programs. Declarative constructs like Sacca and Zaniolo’s choice operator [41] may be useful to provide both a semantics and a syntax for capturing the idea of controlled non-determinism without resorting to operational reasoning.

As discussed in Section 3.4, sometimes the desired solution to non-monotonic code is to implement compensation rather than coordination. Again, the repaired code still contains the original non-monotonic logic, and the program specification is enhanced to achieve some notion of acceptable non-determinism: every customer’s outcome non-deterministically satisfies an exclusive choice among acceptable properties. This bears some resemblance to the previous discussion of choice being made by coordination; it would be interesting if coordination and compensation could be up-leveled to a single more general semantic concept of eventual non-deterministic agreement. With such a concept explicitly identified, perhaps it could be represented linguistically in such a way that repaired programs could be checked for correctness.

4.4 Stochastic CALM

Distributed systems research traditionally deals in deterministic guarantees, often founded in a basis of logic. Recent excitement about machine learning at scale has brought statistical programming concerns to distributed systems. One celebrated result in this space is Hogwild! [40], in which the authors observed empirically—and subsequently proved formally—that a coordination-free parallel implementation of the stochastic gradient descent algorithm is guaranteed to converge to an optimum in the same scenarios as a bulk-synchronous implementation. The proof of this result rests on arguments that do not translate broadly to other programming problems. What is the connection between the specific results of Hogwild! and the general result of the CALM Theorem? Can we broaden our CALM definition of consistency to encompass statistical equivalences like convergence to a near-optimum?

An intriguing result that points in this direction comes from de Sa, et al. [19]. They generalized the idea of Hogwild! and cast their proofs in the frame of super-martingales, in which the current value of a stochastic process is an upper bound on the expected next value: in short, the expectations monotonically shrink. The paper comes up with a stochastic model for algorithms like Hogwild! where the expectations are super-martingales. Perhaps there is a connection between this notion of monotonicity and the logical monotonicity of the CALM Theorem, or the two ideas need to be extended to be brought together.
5 ADDITIONAL RESULTS

The PODS keynote talk that introduced the CALM conjecture included a number of related conjectures regarding coordination, consistency and declarative semantics [29]. Following the CALM Theorem result [9], the database theory community continued to explore these relationships, as summarized by Ameloot [7]. For example, in the batch processing domain, Koutris andSuciu [33], and Beame, et al. [12] examine massively parallel computations with rounds of global coordination, considering not only the number of rounds needed for different algorithms, but also communication costs and skew.

In a different direction, a number of papers tolerate memory inconsistency while maintaining program invariants. Bailsi et al. [11] define a notion of Invariant Confluence for replicated transactional databases, given a set of database invariants. Many of the invariants they propose are monotonic in flavor and echo intuition from CALM. Gotsman et al. [25] present program analyses that identify which pairs of potentially concurrent operations must be synchronized to avoid invariant violations. Li, et al. define RedBlue Consistency [36], requiring that users “color” operations based on their ordering requirements; given a coloring they choose a synchronization regime that satisfies the requirements.

Blazes [2] similarly elicits programmer-provided labels to more efficiently avoid coordination, but with the goal of guaranteeing full program consistency as in CALM.

6 CONCLUSION

Distributed systems theory is dominated by fearsome negative results, such as the Fischer/Lynch/Patterson impossibility proof [22], the CAP Theorem [24], and the two generals problem [26]. These results identify things that are not possible to achieve in any distributed system. As system builders, of course, we are interested in the complement of this space: what can be achieved, and, importantly, how can we achieve it while minimizing complexity and cost?

The CALM Theorem presents a positive result that delineates the frontier of the possible. CALM shows that monotonicity, a property of a program, implies consistency, a property of the output of any execution of that program. The inverse is also established: non-monotonic programs require runtime enforcement (coordination) to ensure consistent execution. As a program property, CALM enables reasoning via static program analysis, and limits or eliminates the use of runtime checks. This is in contrast to storage consistency like linearizability or serializability, which required expensive runtime enforcement.

CALM falls short of being a constructive result—it does not actually tell us how to write consistent, coordination-free distributed systems. Even armed with the CALM theorem, a system builder must answer two key questions. First, and most difficult, is whether the problem they are trying to solve has a monotonic specification. Most programmers begin with pseudo-code of some implementation. The second question is equally important: given a monotonic specification for a problem, how can I implement it in practice? Languages such as Bloom point the way to new paradigms for programming distributed systems that favor (and conservatively) test for monotonic specification. There is remaining work to do making these languages attractive to developers, and efficient at runtime.

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